

1 (optional) (a) prove that the integration of the normal pdf is 1;  
(b) do the same for the exponential pdf; also please find the mean and variance for the random variable of exponential pdf.

2. Matlab simulation problem: it's a simple problem with the following steps:

- (i) Choose an initial random seed, get, say 1000 uniformly distributed random variables. Denote them by  $r_i, i = 1, \dots, n$ .
- (ii) Get a new sequence  $u_i, i = 1, \dots, n$  from  $r_i, i = 1, \dots, n$  by using the rule:  $u_i = 1$  if  $1/2 \leq r_i < 1$ , and  $u_i = -1$ , otherwise.
- (iii) Form  $y_n = \sum_{i=1}^n u_i$ .
- (iv) Get a large number of  $y_n$  by varying the initial random seed; check if the distribution of  $y_n$  follows a normal distribution (Hint: it's a normal distribution with mean 0 and variance  $n$ ).